# Numerical Optimization 01: Introduction

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## Overview



### **2** Why Optimization?

#### 3 Why Julia?





# **Syllabus**

We have two goals:

- Learn Julia programming
- Understand the optimization methods

Subjects to be covered

- Julia programming
- Local Optimization
  - Derivatives and Gradients
  - Bracketing
  - First/second-Order optimization
  - Gradient free methods
  - Stochastic methods
- Global Optimization
- Sampling Plans
- Surrogate Optimization
- Expression Optimization

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Virtual Meet twice a week (90 minutes each time).

- review of homework (20-30 mins)
- lecture (30-50 mins)
- coding (20-30 mins)

# Why optimization

A typical optimization problem is to

minimize f(x)subject to  $x \in X$ 

A design point (x) can be represented as a vector of values corresponding to different design variables.  $\begin{array}{ll} \underset{x_1, x_2}{\text{minimize}} & f(x_1, x_2) \\ \text{subject to} & x_1 \ge 0 \\ & x_2 \ge 0 \\ & x_1 + x_2 \le 1 \end{array}$ 



A necessary condition? for f(x) reaches the minimum is that f'(x) = 0.

## Optimization is hard!

• f'(x) = 0 is not a sufficient condition.



• There exist many points where f'(x) = 0.



• f(x) and f'(x) are hard to evaluate.

## Why Julia?

#### Run Julia at https://www.juliabox.com

- Math-friendly
- Looks like Python
- Runs like C/Fortran
- Growing ecosystem





## Summary

- Optimization in engineering is the process of finding the best system design subject to a set of constraints.
- Optimization can be transformed to a math problem but it is sometimes hard to solve
- We will extensively using the Julia language to learn how to solve the optimization numerically

### Homework

In Julia, write the following trial functions, make the contour plots and analyze their minima behavior.

Booth's function

$$f(x_1, x_2) = (x_1 + 2x_2 - 7)^2 + (2x_1 + x_2 - 5)^2$$

Barnin function

$$f(x_1, x_2) = a(x_2 - bx_1^2 + cx_1 - r)^2 + s(1 - t)cos(x_1) + s$$

where  $a = 1, b = 5.1/(4\pi^2), c = 5/\pi, r = 6, s = 10, t = 1/8\pi$ .

Rosenbrock's Banana function

$$f(x_1, x_2) = (a - x_1)^2 + b(x_2 - x_1^2)^2$$

where a = 1, b = 5.

More functions can be found at https:

//en.wikipedia.org/wiki/Test\_functions\_for\_optimization